

Caythorpe Primary School



Mathematics Policy

Purpose: This policy reflects the values and philosophy of the school in relation to the teaching and learning of Mathematics at Caythorpe Primary School

Audience: This policy has been devised by the whole staff and adopted by the governors.

September 2021

Review date: September 2022

Maths Policy 2021

INTRODUCTION

This Maths and Calculation Policy has been produced in line with the 2014 National Curriculum for Mathematics to ensure consistency and progression in teaching throughout the school that is age appropriate. It aims to introduce children to the processes of calculation through practical, oral and mental activities. As children begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, use particular methods that apply to special cases and learn to interpret and use signs and symbols involved. This policy shows the natural progression that a child should make in their mathematical education. Children should not progress onto the advanced stages of formal written methods until they have a secure conceptual understanding. By the end of Year 6, children should be able to choose the most appropriate approach to solve a problem: making a choice between using jottings (an extended written method), an efficient written method or a mental method.

Intent

Maths is a journey and long-term goal, achieved through exploration, clarification, practice and application over time. At each stage of learning, children should be able to demonstrate a deep, conceptual understanding of the topic and be able to build on this over time.

Our overall aims for when children leave Caythorpe Primary School, are:

- develop a positive attitude to mathematics as an interesting and attractive subject in which all children gain success and pleasure.
- have access to a high quality maths curriculum that is both challenging and enjoyable, and builds upon previous learning.
- be provided with a variety of mathematical opportunities, which will enable them to make the connections.
- ensuring children are confident mathematicians who are not afraid to take risks.
- develop an ability to express themselves fluently, to talk about the subject with assurance, using correct mathematical language and vocabulary.
- develop mathematical skills and knowledge and recall of basic facts and the four operations
- be able to use this knowledge and understanding to carry out calculations mentally
- make use of diagrams and informal notes to help record steps and part answers when using mental methods that generate more information than can be kept in their heads
- have an efficient, reliable, compact written method of calculation for each operation that children can apply with confidence when undertaking calculations that they cannot carry out mentally. They will do this by always asking themselves: Can I do this in my head? Can I do this in my head using drawings or jottings? Do I need to use a pencil and paper procedure of a formal written method?

Implementation

Our implementation is developed through secure understanding of the curriculum and subject area.

Planning

Maths is a core subject in the National Curriculum. Caythorpe follows the White Rose Maths scheme to support children in their learning journey as by following the Mastery approach will help to avoid gaps in their learning after time. Teachers also have access to a variety of websites and planning to support their planning process which enables them to find high quality Maths resources to allow children to further develop their Maths Talk language and to develop their confidence to reason and solve problems.

Planning is undertaken at three levels:

1. Long term: National Curriculum

The National Curriculum 2014 has 3 central aims:

- Become **fluent** in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately. In order to achieve this we need to provide opportunities for children to investigate numbers by counting, cardinality (how many there are in the group), comparison and composition. They need to practice decomposing and recomposing numbers, recalling number bonds and multiplication tables to improve mathematical fluency.
- **Reason mathematically** by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language. The conversations we have and questions we ask are key to developing reasoning skills. We can ask children to describe, explain, convince others, justify and prove to promote their reasoning skills. Adults can support children to develop reasoning by modelling, using mathematical language (also displayed in classrooms), using sentence stems (displayed and referred to on the front covers of the Maths books), group work, understanding how others work and making personal notes and recordings.
- Can **solve problems** by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions. Activities should be provided where children can solve number problems, practical problems and missing number problems. Problem solving is not just about solving the problem, it is about how they solved the problem. What strategies and mathematical concepts did they use? All pupils should have the opportunity to apply their mathematics to solve problems. The use of mathematical language, modelling and the bar model can all help support children to develop their problem solving skills. Higher attaining children need to solve problems that require more demanding reasoning and problem solving skills rather than harder numbers. We must ensure that children have the opportunity to conjecture when problem solving. Problem solving is more than learning and following a procedure.

2. Medium term

The sequencing of teaching reflects the needs of the learners. Place value and arithmetic are given priority at the start of each academic year as these are the building blocks for mathematical learning. Here on, it is an ongoing formative assessment and analysis process of curriculum objects (use of Pupil Asset) that results in the learning being planned for and delivered in direct correlation to the children's ability, starting point and individual next steps.

3. Short term planning

Short term planning is carried out weekly by the class teacher supported by the use of many different websites and our Calculation Policy. These plans list the specific learning objectives and details of how the lessons are to be taught, including key vocabulary and resources required.

- Daily lessons include a clear lesson intention 'WALT' and clear success criteria 'Steps to Success'.

- Daily lessons are taught using development of Maths Talk language, group work, partner work which then leads to the confidence in individual work.

Concrete, pictorial and Abstract (CPA) approach

At Caythorpe, we recognise that the **Concrete Pictorial Abstract (CPA)** approach is highly effective in the teaching of Maths to develop conceptual understanding. This approach will vary between year groups and the individual abilities of children within each class.

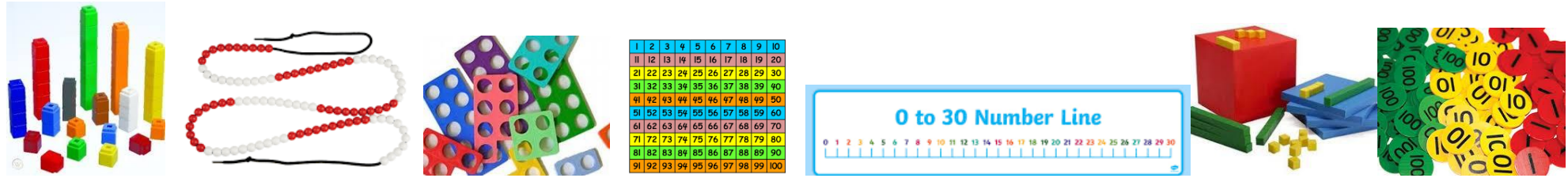
Objects, pictures, words, numbers and symbols are everywhere. The mastery approach incorporates all of these to help children explore and demonstrate mathematical ideas, enrich their learning experience and deepen understanding. Together, these elements help cement knowledge so pupils truly understand what they've learnt.

All pupils, when introduced to a key new concept, should have the opportunity to build competency in this topic by taking this approach. Pupils are encouraged to physically represent mathematical concepts. Objects and pictures are used to demonstrate and visualise abstract ideas, alongside numbers and symbols.

Concrete – The doing stage

There is a clear focus on the use of manipulatives and visual images to support understanding in every year group. Each new concept or calculation strategy will be introduced using appropriate manipulatives, giving the children a clear picture of the theoretical mathematics they are learning. It is important that children have access to a wide range of manipulatives in every year group and, consequently, we encourage children to be independent in their use of manipulatives throughout the school and access resources as they see fit. This is the foundation for conceptual understanding.

Concrete resources that may be found in classrooms will include:



These resources will vary depending on year group and individual needs.

Pictorial – The seeing stage

A child has sufficiently understood the hands-on experiences performed and can now relate them to representations, such as a diagram or a picture of the problem.

Abstract- The symbolic stage

A child is now capable of representing problems by using mathematical notation, for example $10 \div 2 = 5$

Teaching

'Quality first teaching' linked to teaching standards:

All teachers:

1. 'Know where their children are' through the use of summative assessment, prior learning, assessment, maths talk

2. 'Understand where their children need to be' through a secure understanding of year group expectations and/or pre key stage expectations and ongoing, formative assessment
3. 'Know how they are going to get them there' through the use of a range of strategies to promote independence, mastery and high expectations of ALL.
4. Effectively deploy adults, specifically during introductions, plenaries & catch-up sessions
5. Plan for progression during and between lessons which includes making sure that children have an opportunity to move beyond the fluency stage onto the reasoning and problem solving or 'deeper thinking' tasks.

Impact

Pupils will leave us prepared for the next stage in their lives with:

- Quick recall of facts and procedures
- The flexibility and fluidity to move between different contexts and representations of mathematics
- The ability to recognise relationships and make connections in mathematics
- Confidence and belief that they can achieve
- The knowledge that maths underpins most of our daily lives
- Skills and concepts that have been mastered
- Have a positive and inquisitive attitude to mathematics as an interesting and attractive subject in which all children gain success and pleasure.

A mathematical concept or skill has been mastered when a child can show it in multiple ways, using the mathematical language to explain their ideas, and can independently apply the concept to new problems in unfamiliar situations and this is the goal for our children.

Assessment

These will be assessed through: assessment, tracking, pupil progress meetings, performance management, moderation and standardisation.

Marking WALTs and steps to success are shared with the children in every lesson. Children are provided with opportunities for self/peer-assessment and improvement.

Marking is developmental and children are provided with next steps to extend their learning at least weekly. Teachers monitor the acquisition of skills, knowledge and understanding through appropriate teacher intervention, observations and discussions with groups and individuals. We see assessment as an integral part of the teaching process and strive to make our assessment purposeful, allowing us to match the correct level of work to the needs of the pupils, thus benefiting the pupils and ensuring progress

Summative assessment - Are carried out on a termly basis using the Star assessment. This is used to inform future planning and intervention sessions as the STAR assessment system provides teachers with an in-depth analysis on each child whilst also helping to identify key children in need of intervention and the White Rose Maths end of term assessments allows teachers to identify any gaps in the children's learning so that these can be filled to improve their knowledge.

Times Tables Rockstars (TTRS) has been bought and is being implemented from Y2-6 to aid children in preparation for the Y4 times table check. Children are encouraged to play at home on a regular basis. The numeracy coordinator is responsible for delivering an assembly once every term to encourage children to play at home whilst also rewarding those who play regularly as an incentive to others.

Pupil Progress meetings- Are held termly between the class teacher, subject leader and/or SENDCo (Special Needs Coordinator) and Headteacher. At these meetings the children's progress and attainment are discussed. Therefore, achievement and attainment in mathematics are being carefully monitored and analysed not only by the maths

subject leader but also the class teacher, SENDCo and Head teacher. Furthermore, all assessment data is available for staff to view on Integris. Assessment is regarded as an integral part of teaching and learning and is a continuous process. It is the responsibility of the class teacher to assess all pupils in their class.

Roles in learning

Maths Leader

The Maths subject leader is responsible for co-ordinating mathematics through the school. This includes:

- inspiring an exciting and creative approach to maths teaching
- supporting maths teaching through advice, guidance, PD and resources
- sharing information acquired from courses or other sources that may be beneficial to staff
- reviewing the maths policy and monitoring its implementation
- regularly evaluating the maths scheme of work and amending as necessary
- the management, maintenance and storage of resources
- organising pupils' participation in maths workshops and events
- effectively managing the maths budget
- reporting to parents, governors and others when appropriate

Class Teacher

- to deliver quality-first teaching to the children making sure progression in the acquisition of mathematical skills with due regard to the National Curriculum for mathematics
- to develop and update skills, knowledge and understanding of mathematics
- to identify inset needs in mathematics and take advantage of training opportunities
- to keep appropriate on-going records
- to plan effectively for mathematics liaising with manager when necessary.
- to inform parents of pupils' progress, achievements and attainment

Parental Involvement

At our school we have an open-door policy and encourage parents to become involved in their children's mathematical learning.

At Caythorpe Primary School we encourage parents to be involved by:

- visiting them into school twice yearly to discuss the progress of their child
- inviting parents into school in the summer term to discuss the yearly report
- making parents aware and encouraging them to aid their child in their learning.
- encouraging parents to help in classrooms

- inviting parents to come into workshops for parents focusing on areas of mathematics

Governing Body

Governors are invited into school on a regular basis to observe lessons. They are also encouraged to speak with children about their learning and to look at books to see what the children have been covering in lessons.

*Where classes contain a mixed year group the teacher chooses objectives within the units that are the most appropriate for their class, taking into account age, ability and past experience of the children.



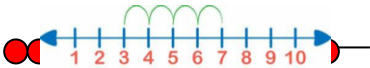


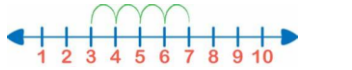



**Mathematics is taught as a discreet subject but also contributes to other subject areas and it is important the children are given opportunities to apply and use Mathematics in real contexts. 'It is important that time is found in other subjects for pupils to develop their Numeracy Skills, e.g. there should be regular, carefully planned opportunities for measuring in science and technology, for the consideration of properties of shape and geometric patterns in technology and art, and for the collection and presentation of data in history and geography. Our topic-based approach supports the use of mathematical skills throughout the curriculum encouraging children to understand the importance of the subject and to apply skills in a practical situation.






***In the EYFS mathematics forms a fundamental part of the day through child-initiated learning. Group activities in Foundation last between 10-15 minutes.



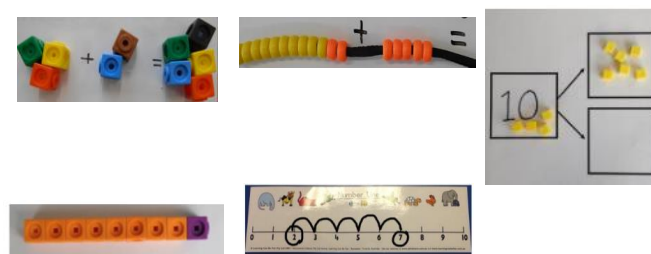
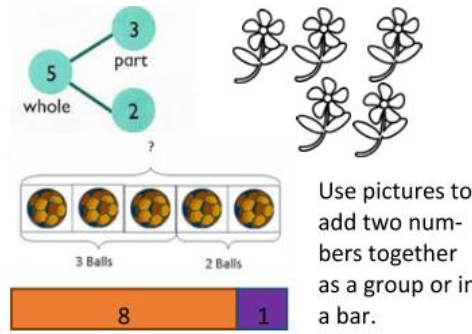
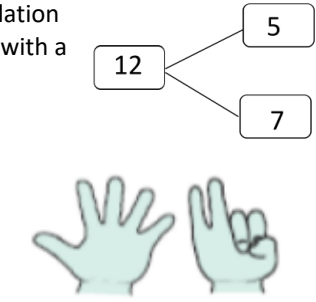
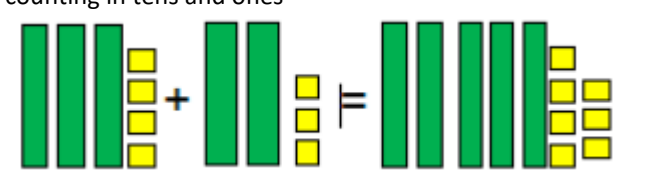
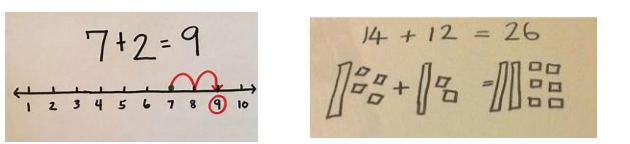
Calculation Policy 2021

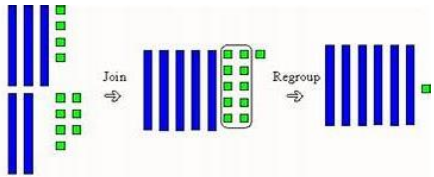

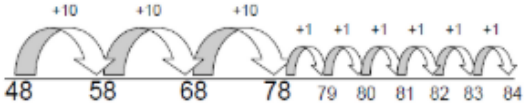
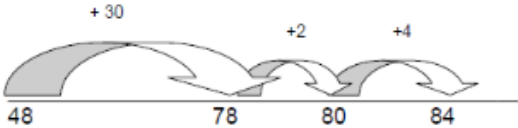
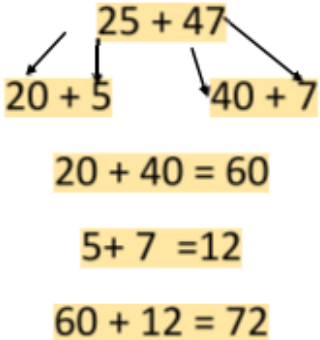
EYFS (Reception)

Addition	Subtraction	Multiplication	Division
<p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects.</p>  <p>They combine objects in practical ways and count all.</p>  <p>They understand addition as counting on and will count on in ones and twos using objects, cubes, bead string and number line.</p>  <p>They use concrete and pictorial representation to record their calculations.</p>	<p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects.</p>  <p>They understand subtraction as counting out.</p>  <p>They begin to count back in ones and twos using objects, cubes, bead string and number line.</p>  <p>They use concrete and pictorial representation to record their calculations.</p>	<p>Children use concrete objects to make and count equal groups of objects.</p>  <p>They will count on in twos using a bead string and number line.</p> <p>They understand doubling as repeated addition.</p> $2 + 2 = 4$ <p>They use concrete and pictorial representation to record their calculations. Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p> 	<p>Children use concrete objects to count and share equally into 2 groups.</p> <p>6 cakes shared between 2 people each person gets 3 cakes. $6 \div 2 = 3$</p>  <p>They count a set of objects and halve them by making two equal groups.</p> <p>They understand sharing and halving as dividing by 2.</p> <p>They will begin to use objects to make groups of 2 from a given amount.</p> <p>They use concrete and pictorial representation to record their calculations.</p>

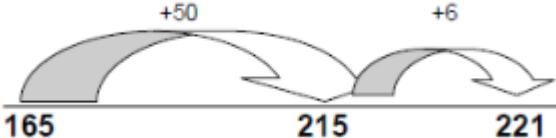
<p>They begin to use + and = </p> <p>They are encouraged to develop a mental picture of the number system in their heads to use for calculations.   </p> <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>	<p>They begin to use - and =</p> <p>They are encouraged to develop a mental picture of the number system in their heads to use for calculations.</p> <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>		 <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>
--	---	--	---

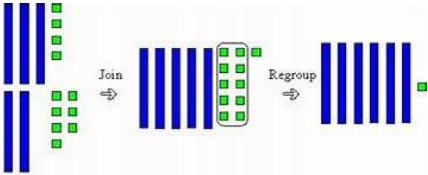
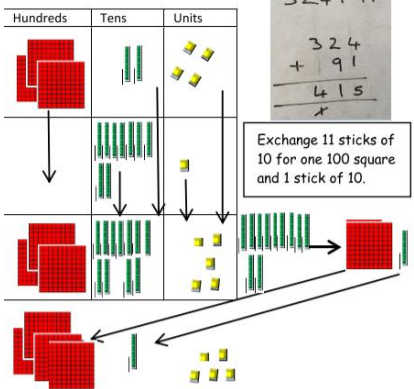
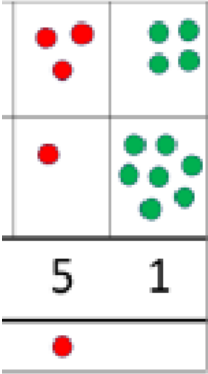

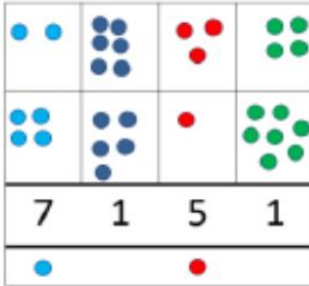
Calculation Policy

ADDITION - KS1 (Years 1&2)			
	Concrete	Pictorial	Abstract
S t a g e 1	<p>Use part part whole model, cubes and bead strings to add two numbers together as a group or in a bar.</p> 	<p>Use jottings to represent numbers.</p>  <p>Use pictures to add two numbers together as a group or in a bar.</p>	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p>  <p>$11 + 4 = 15$</p> <p>They may use their fingers to support their mental methods</p> <p style="text-align: center;"><u>5 + 2 = 7</u></p>
S t a g e 2	<p>Grouping objects to add</p> <p>Children will use dienes cubes to add larger numbers where regrouping is not required.</p> <p>They will also use a bead string to add larger numbers by counting in tens and ones</p> 	<p>Number line</p> <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer. Children will show their representations from the concrete method using pictures.</p>  <p>Numbers will get progressively larger throughout the keystage. Children will be able to add tens and ones using</p>	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p style="text-align: right;">$27 + 10 = 37$</p> <p style="text-align: right;">$27 + 20 = 47$</p> <p>Children will begin to add multiples of tens.</p> <p style="text-align: right;">$27 + \square = 57$</p>

		<p>an empty number line.</p>	
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Stage 3</p>	<p>Partitioning Children will add larger numbers where they will need to join, regroup and count.</p>  <p>Children will also use bead strings to add numbers together using groups of tens and ones to count on.</p> 	<p>Number line Use an empty number line to count in tens and then ones.</p>  <p>When confident:</p> 	<p>Partitioning Children will begin to use the partitioning method. Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total.</p> 

Calculation Policy

ADDITION - Lower KS2 (Years 3 & 4)			
	Concrete	Pictorial	Abstract
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Stage 1</p>	<p>Use dienes cubes to consolidate learning from KS1. Ensure children are confident at using these to join, regroup and count. This will support them moving onto the next stage of column addition.</p>	<p>Number line Consolidate their learning from KS1 by using an empty number line to count larger numbers.</p> 	<p>Partitioning Children will consolidate using the partitioning method. The layout will begin to form a written method to support further progress onto the column method. Hundreds, Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total.</p>

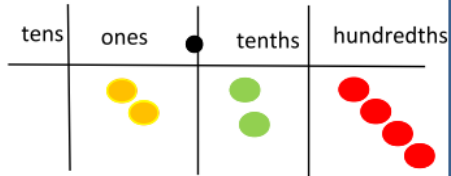
			$\begin{array}{r} 200 \\ + 100 \\ \hline 300 \end{array} \quad \begin{array}{r} + 60 \\ + 10 \\ \hline 70 \end{array} \quad \begin{array}{r} + 3 \\ + 9 \\ \hline 12 \\ + 2 \\ \hline 14 \end{array}$
Stage 2	<p>Introduce children to place value counters and dienes cubes. Use the column method layout to support their learning onto the abstract method.</p> 	<p>Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line.</p> 	<p>Expanded column method - Formal method Children to use the Expanded Column Method. Start by partitioning the numbers before the formal column to show the exchange. Once confident, they can move onto the column method in stage 3.</p> $\begin{array}{r} 176 \\ + 147 \\ + 13 \\ + 110 \\ \hline 323 \end{array} \quad \begin{array}{l} (7+6) \\ (70+40) \\ (100+100) \end{array} \quad \begin{array}{r} 147 \\ + 176 \\ \hline 323 \end{array}$
Stage 3	<p>Children will add larger numbers where they will need to exchange place value counters or dienes cubes.</p> 	<p>Children can draw a representation of the grid using larger numbers.</p> 	<p>Column method - Formal method Column Method for addition to be used.</p> $\begin{array}{r} 4478 \\ + 3762 \\ \hline 8240 \\ \hline 111 \end{array}$

Calculation Policy

ADDITION - Upper KS2 (Years 5 & 6)

Concrete	Pictorial	Abstract
----------	-----------	----------

Introduce decimal place value counters and model regrouping for addition.



Children will draw their representations showing where they have regrouped.

2.37 + 81.79

40,265 43,265 □ □ □

TTh	Th	H	T	O
4	0	2	6	5
+	3	5	2	2

Column method

Children will continue to develop their understanding of column method addition. Calculations will become larger and include decimal places.

$$\begin{array}{r} 379.173 \\ + 203.116 \\ \hline 582.289 \end{array}$$

Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.

Children will begin to use the bar model when problem solving. Jottings and calculations should be recorded to show their processes.

Column method

Children to further develop their confidence using the column method. Larger numbers, decimal places and inserting zero for place holders when decimals are different.

6 digit + 6 digit

$$\begin{array}{r} 447813 \\ + 376245 \\ \hline 824058 \end{array}$$

Numbers with 3 decimal place

$$\begin{array}{r} 379.173 \\ + 203.116 \\ \hline 582.289 \end{array}$$

Numbers with a different number of decimal places

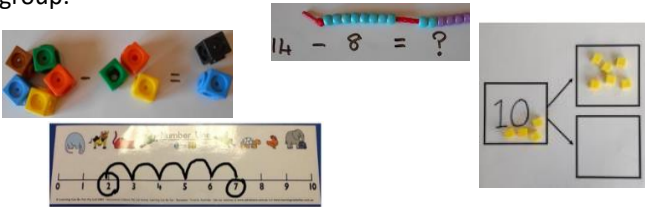
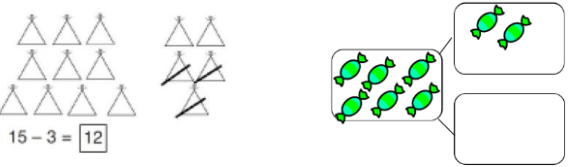
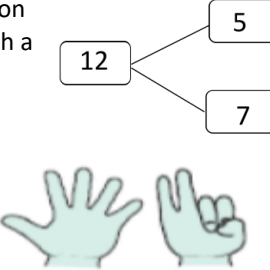
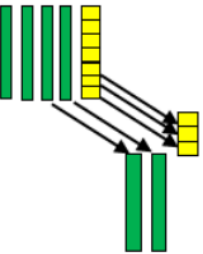
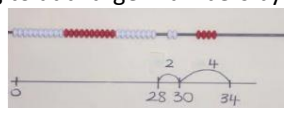
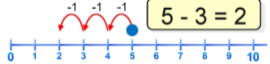
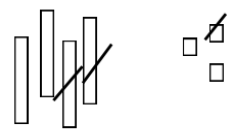
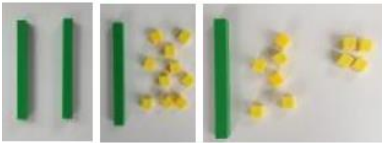
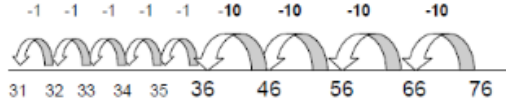
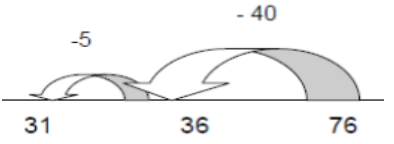
45.25 + 8.5 + 3.247

$$\begin{array}{r} 45.250 \\ + 8.500 \\ + 3.247 \\ \hline 56.997 \end{array}$$

Insert zeros for place holders.

$$\begin{array}{r} 23.361 \\ 9.080 \\ 59.770 \\ + 1.300 \\ \hline 93.511 \end{array}$$

Calculation Policy

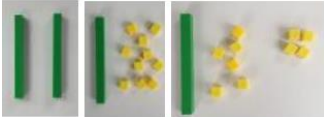
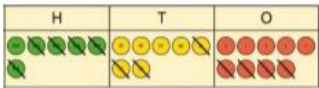
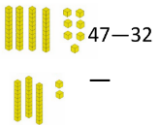
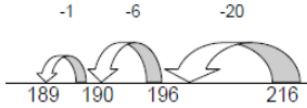
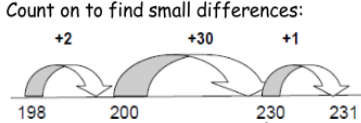
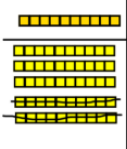
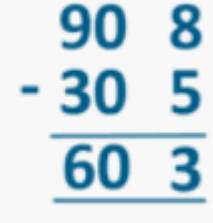
	Concrete	Pictorial	Abstract
Stage 1	<p>Taking objects away Use part whole model, cubes and bead strings to subtract two numbers together by moving objects away from the group.</p> 	<p>Use jottings to represent numbers. Children will learn to cross out drawn objects to show what has been taken away.</p> 	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p>$11 - 4 = 7$</p> <p>They may use their fingers to support their mental methods</p> 
Stage 2	<p>Children will use dienes cubes to subtract larger numbers where exchanging is not required. Children will lay out the first number using the dienes cubes and then move the second number away to show the subtraction.</p>  <p>They will also use a bead string to add larger numbers by counting in tens and ones.</p> 	<p>Number line Children will begin to draw their own number lines. Start at the larger number on the number line and count back in ones or in one jump to find the answer.</p>  <p>Numbers will get progressively larger throughout the keystage. Children will be able to subtract tens and ones using an empty number line.</p>  <p>Children will show their representations from the concrete method using pictures.</p> <p>$43 - 21 = 22$</p>	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p>$25 - 12 = 13$</p> <p>Children will begin to subtract multiples of tens.</p> <p>$25 - 10$ $25 - 10 = 15$</p>
Stage 3	<p>Children will begin to use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones.</p> 	<p>Empty number line -Use an empty number line to count back in tens and then ones.</p>  <p>When confident:</p> 	<p>Partitioning method Children will begin to use the partitioning method. Tens and ones will be subtracted to form partial sums and then these partial sums will be added together to find the total.</p> <p>$47 - 23 = 24$ $47 - 20 = 27$ $27 - 3 = 24$</p>

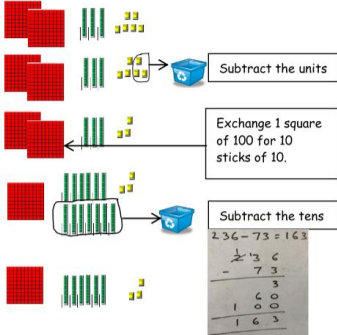
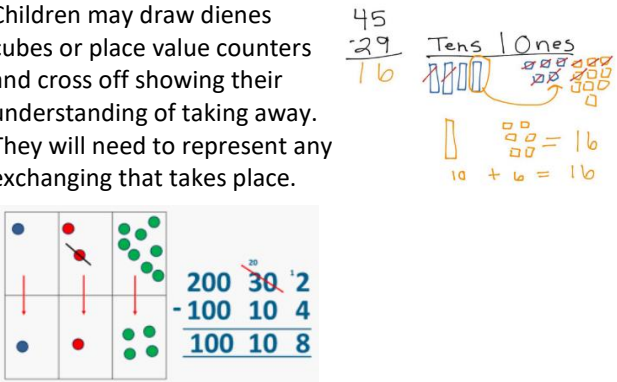
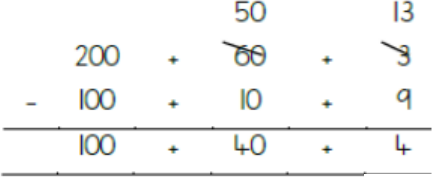
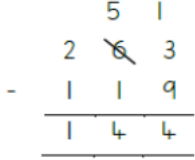

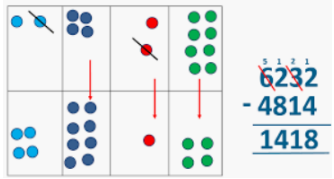
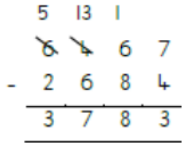
$$47 - 24 = 23$$

$$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$$

Calculation Policy

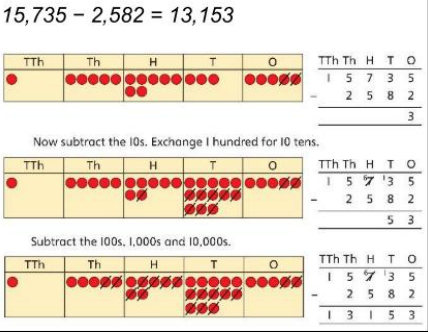
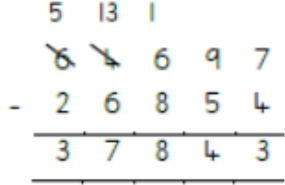
SUBTRACTION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
S t a g e 1	<p>Children consolidate and use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones.</p>  <p>They will be able to begin to lay this out like the column method and removing counters or cubes away to represent taking away.</p>  	<p>Consolidate their learning from KS1 by using an empty number line to calculate larger numbers.</p> <p>Children will also be able to draw representations of dienes cubes and place value counters by crossing out the number being taken away.</p> <p>Develop the use of empty number line with calculations that bridge 100:</p>  <p>Count on to find small differences:</p>   <p>Calculations</p> $\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$	 $47 - 24 = 23$ $\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$ <p>Children to further secure their knowledge using the partitioning method but will start to lay their work out using the column method approach. Tens and ones will be subtracted to form partial sums and then these partial sums will be added together to find the total.</p>

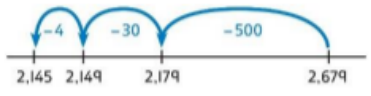
S t a g e 2	<p>Children begin to set out HTU - HTU using dienes cubes and place value counters (that cross the tens boundary) in columns and record as column subtraction with decomposition. Teach children how to exchange units of numbers.</p> 	<p>Children may draw dienes cubes or place value counters and cross off showing their understanding of taking away. They will need to represent any exchanging that takes place.</p> 	<p>Partitioning method - with exchanging Children will use the partitioning method to show exchanging.</p>  <p>Once confident, children can start to use the column method.</p> 
S t a g e 3	<p>Children continue to develop their confidence in using dienes cubes and place value counters to show decomposition using the column method.</p> 	<p>Children draw representations from concrete activities using dienes cubes and place value counters.</p> 	<p>Column Method Children continue to use column method to subtract larger numbers.</p> 

Calculation Policy

SUBTRACTION - Upper KS2 (Years 5 & 6)

	Concrete	Pictorial	Abstract
S t a g e 1	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.</p>	<p>Children can draw using place value counters showing how exchanging takes place between the units of numbers.</p>  <p>Children also show subtraction on an empty number line</p>	<p>Column Method Children will continue to develop their understanding of column method subtraction. Calculations will become larger.</p> <p>5 digit - 5 digit</p> 

		using larger numbers.	
--	--	-----------------------	--



Introduce decimal place value counters and model exchange for subtracting between units of numbers.

$5.74 - 2.25 = ?$

O	•	Tth	Hth	O · Tth Hth
●●●●●	•	●●●●●	●●●●●	5.74
●●●●●	•	●●●●●	●●●●●	-2.25
-				
.				

Exchange 1 tenth for 10 hundredths.

O	•	Tth	Hth	O · Tth Hth
●●●●●	•	●●●●●	●●●●●	5.74
●●●●●	•	●●●●●	●●●●●	-2.25
-				
.				

Now subtract the 5 hundredths.

O	•	Tth	Hth	O · Tth Hth
●●●●●	•	●●●●●	●●●●●	5.74
●●●●●	•	●●●●●	●●●●●	-2.25
-				
.				
9				

Now subtract the 2 tenths, then the 2 ones.

O	•	Tth	Hth	O · Tth Hth
●●●●●	•	●●●●●	●●●●●	5.74
●●●●●	•	●●●●●	●●●●●	-2.25
-				
.				
3 · 4 9				

Children will draw their representations showing where they have exchanged.

A place value chart with columns for 1s, 10s, 100s, and 1000s. The number 4.264 is written in black, and 2.437 is written in red below it. The subtraction is shown as $4.264 - 2.437 = 1.827$. The chart shows the exchange of 1 ten for 10 ones and 1 hundred for 10 tens.

Children will continue to develop their understanding of column method subtraction. Calculations will become larger, include decimal places and require 0 to be added as a placeholder.

6 digit - 6 digit

$$\begin{array}{r} 5131 \\ - 268514 \\ \hline 378423 \end{array}$$

Numbers with 3 decimal place

$$\begin{array}{r} 73.798 \\ - 216.273 \\ \hline 527.525 \end{array}$$

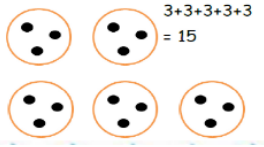
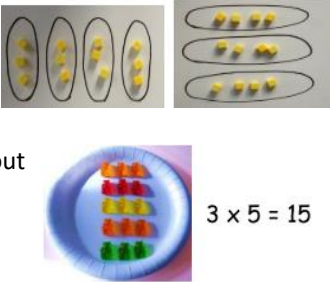
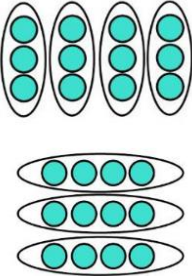

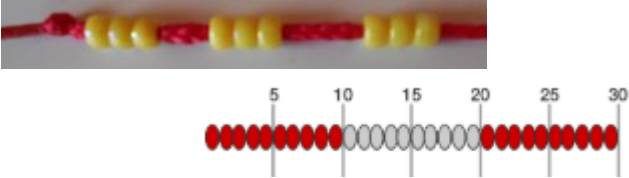
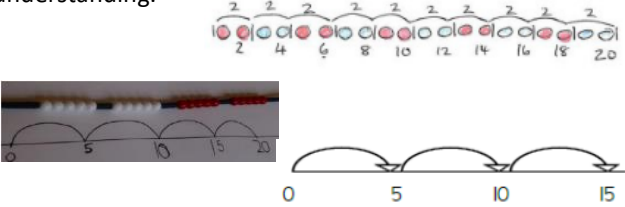
Numbers with a different number of decimal places

$$69.2 - 27.54 = 41.66$$

Calculation Policy

MULTIPLICATION - KS1 (Years 1&2)

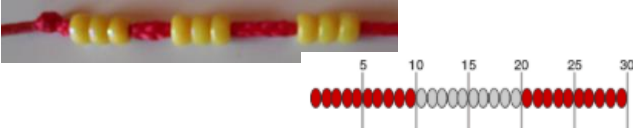
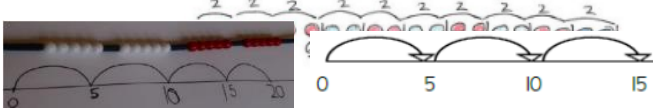
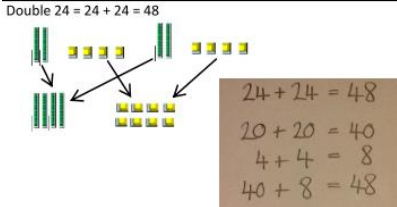
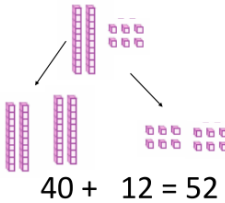
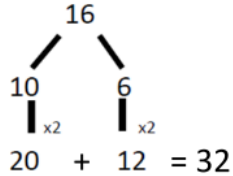
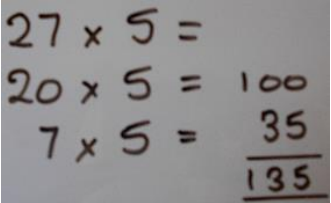
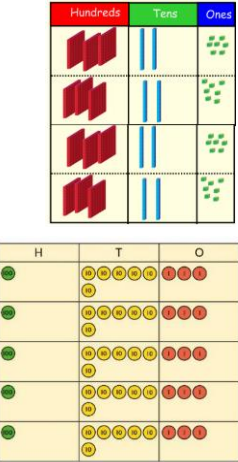
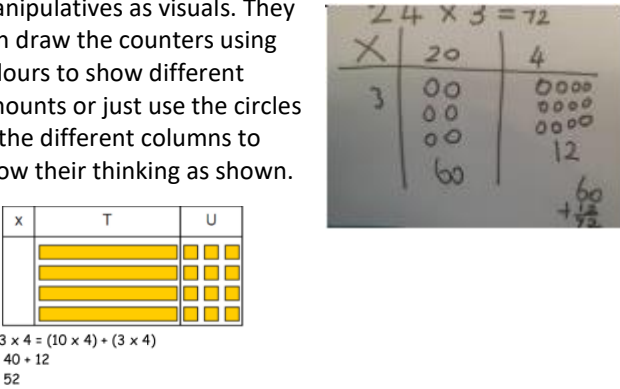
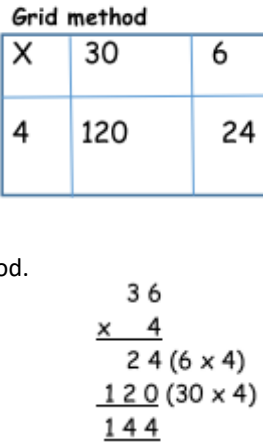
	Concrete	Pictorial	Abstract
S t a g e 1	<p>Repeated addition - Groups of multiple objects</p> <p>Children will count groups of the same number of objects and add them together. The children learn about grouping in practical contexts and through pictorial representations.</p>	<p>Children draw representations to show counting in multiples and groups.</p> <p>Double 4 is 8</p>	<p>Children show multiplication as repeated addition. Children may provide pictorial representations to support.</p> <p>3×9</p> <p>$3 + 3 + 3 = 9$</p>

			
S t a g e 2	<p>Arrays Children will be able to represent a multiplication calculation using an array and write the multiplication symbol within a number sentence. Children will also understand that multiplication can be carried out in any order (commutative).</p>  <p>$3 \times 5 = 15$ $5 \times 3 = 15$</p>	<p>Children draw representations to show arrays.</p> 	<p>Children use arrays to show how to solve multiplication calculations. Children are able to show that multiplication can be done in any order (commutative).</p> <p>$3 \times 5 = 15$ $5 \times 3 = 15$</p> <p>Introduce x sign and record as number sentence</p> <p>$7 \times 10 = 70$ $4 \times 5 = 20$</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p>$5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$</p>
S t a g e 3	<p>Number line Children will understand the operation of multiplication as repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadsting concrete resources may be used to support conceptual understanding.</p> 	<p>Children show multiplication as repeated addition.</p> <p>$5 + 5 + 5 = 15$</p> <p>Introduce x sign and record as number sentence</p> <p>$7 \times 10 = 70$ $4 \times 5 = 20$</p>

Calculation Policy

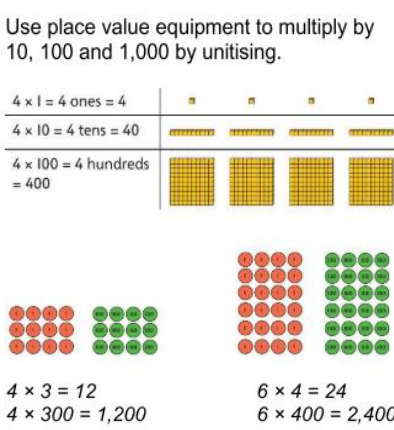
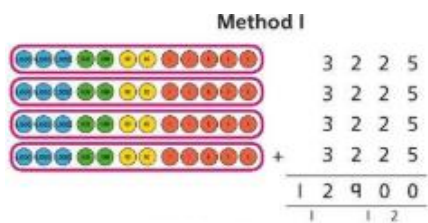
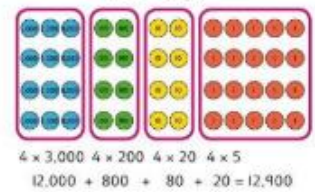
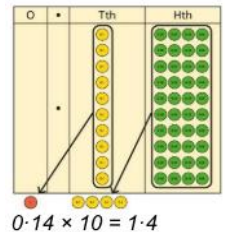
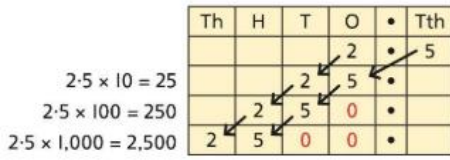
MULTIPLICATION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
S t	<p>Number line - Consolidation Children will understand the operation of multiplication as</p>	<p>Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadsting</p>	<p>Children show multiplication as repeated addition.</p>

<p>a g e 1</p>	<p>repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>concrete resources may be used to support conceptual understanding.</p> 	<p>$5 + 5 + 5 = 15$</p> <p>Introduce x sign and record as number sentence</p> <p>$7 \times 10 = 70$</p> <p>$4 \times 5 = 20$</p>
<p>S t a g e 2</p>	<p>Partitioning Children will learn to multiply ones and tens separately before recombining the numbers back together. They can use Dienes cube of place value counters to achieve this.</p> 	<p>Children can draw representations of the partitioning process to support their conceptual understanding.</p> 	<p>Partition a number and then multiply each part before recombining it back together.</p>  
<p>S t a g e 3</p>	<p>Grid Method Show the links with arrays to first introduce the grid method. Move onto Dienes cubes to move towards a more compact method. Move on to place value counters to show how we are finding groups of a number. We are multiplying by 5 so we need 5 rows of that number.</p> 	<p>Pictorial representations can be made using their concrete manipulatives as visuals. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown.</p> 	<p>Children should be able to draw the grid method for each multiplication. The grid method will be used to show how this relates to a formal written method.</p> <p>Grid method may then lead to the expanded method.</p> 

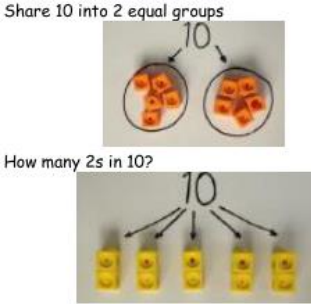
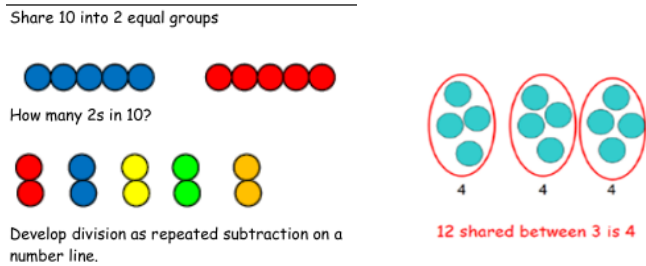


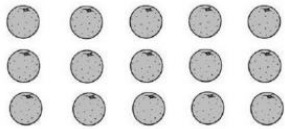
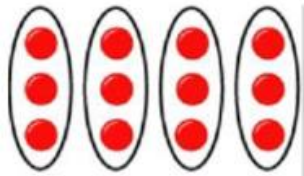
Calculation Policy

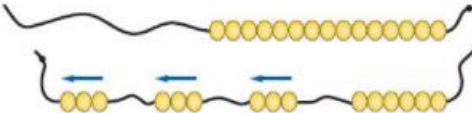
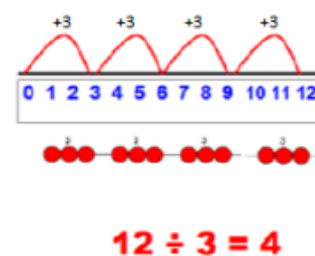
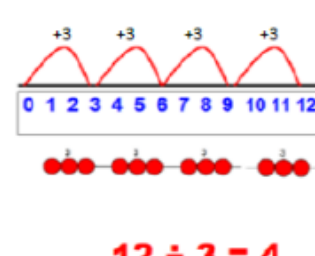
MULTIPLICATION - Upper KS2 (Years 5 & 6)

	Concrete	Pictorial	Abstract						
Stage 1	<p>Concrete materials may be needed to support children's conceptual understanding. Dienes cubes and place value counters will support.</p> <p>Use place value equipment to multiply by 10, 100 and 1,000 by unitising.</p> <p>When multiplying by 10,100,1000 initial concrete resources will be used to support understanding.</p>  <p> $4 \times 1 = 4 \text{ ones} = 4$ $4 \times 10 = 4 \text{ tens} = 40$ $4 \times 100 = 4 \text{ hundreds} = 400$ </p> <p> $4 \times 3 = 12$ $4 \times 300 = 1,200$ </p> <p> $6 \times 4 = 24$ $6 \times 400 = 2,400$ </p>	<p>Use place value equipment to compare methods.</p> <p>Method 1</p>  <p>Method 2</p>  <p> $4 \times 3,000 = 12,000$ $4 \times 200 = 800$ $4 \times 20 = 80$ $4 \times 5 = 20$ $12,000 + 800 + 80 + 20 = 12,900$ </p>	<p>The grid method may be used to show how this relates to a formal written method. Grid method will lead onto expanded method and then onto the compact short multiplication.</p> <p>Grid method</p> <table border="1" data-bbox="1478 319 1758 470"> <tr> <td>X</td> <td>30</td> <td>6</td> </tr> <tr> <td>4</td> <td>120</td> <td>24</td> </tr> </table> <p>Leading to expanded method</p> $\begin{array}{r} 36 \\ \times 4 \\ \hline 24 \text{ (6} \times 4\text{)} \\ 120 \text{ (30} \times 4\text{)} \\ \hline 144 \end{array}$ <p>→</p> $\begin{array}{r} 36 \\ \times 4 \\ \hline 144 \\ 2 \end{array}$ <p>Use known facts and unitising to multiply.</p> <p> $5 \times 4 = 20$ $5 \times 40 = 200$ $5 \times 400 = 2,000$ $5 \times 4,000 = 20,000$ </p>	X	30	6	4	120	24
X	30	6							
4	120	24							
Stage 2	<p>When multiplying decimals by 10,100,1000 initial concrete resources will be used to support understanding to show how exchanging can take place.</p>  <p> $0.14 \times 10 = 1.4$ </p>	<p>This pictorial grid method will support children's understanding of multiplying by 10, 100, 1000.</p>  <p> $2.5 \times 10 = 25$ $2.5 \times 100 = 250$ $2.5 \times 1,000 = 2,500$ </p>	<p>Long multiplication</p> <p>Children may wish to use 2 separate calculations to support their understanding. Reinforce language of place value when multiplying by multiples of 10. Extend to 3 or 4-digit numbers multiplied by a 2-digit number.</p> $\begin{array}{r} 23 \\ \times 13 \\ \hline + 69 \text{ (3} \times 23\text{)} \\ 230 \text{ (10} \times 23\text{)} \\ \hline 299 \end{array}$						
Stage 3	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.</p>	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.</p>	<p>Use column multiplication, ensuring understanding of place value at each stage.</p> $\begin{array}{r} 1.43 \\ \times 6 \\ \hline 8.58 \\ \hline 21 \end{array}$ $\begin{array}{r} 1274 \\ \times 32 \\ \hline 2548 \text{ (1,274} \times 2\text{)} \\ 38220 \text{ (1,274} \times 30\text{)} \\ \hline 40768 \text{ (1,274} \times 32\text{)} \\ \hline 1,274 \times 32 = 40,768 \end{array}$						

Calculation Policy

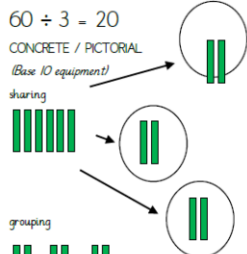

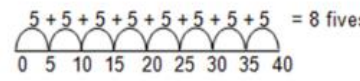
DIVISION - KS1 (Years 1&2)

	Concrete	Pictorial	Abstract
S t a g e 1	<p>Sharing and Grouping Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p> 	<p>Use pictures to share objects. Use circles rather than dots to aid counting.</p> <p>Share 10 into 2 equal groups</p>  <p>Develop division as repeated subtraction on a number line.</p>	<p>Children will be able to represent a division calculation using a pictorial method and write the division within a number sentence.</p> <p>$10 \div 2 = 5$</p> <p>Share 10 into 2 equal groups</p> 
S t a g e 2	<p>Arrays Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p>  <p>Eg: $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$</p>	<p>Draw arrays to show how pictures are divided.</p> 	<p>Children will be able to represent a division calculation using an array and write the division within a number sentence</p> <p style="text-align: center;">$12 \div 3 = 4$</p> 

S t a g e 3	<p>Repeated addition and subtraction</p> <p>Children will understand the operation and repeated addition or subtraction using bead strings and number lines. This will support the pictorial element.</p> <p style="text-align: center;">$15 \div 3 = 5$</p> 	<p>Children will understand the operation of division as grouping using repeated addition or subtraction on a prepared number line.</p>  <p style="text-align: center;">$12 \div 3 = 4$</p>	<p>Children will be able to represent a division calculation using a numberline and write the division within a number sentence.</p>  <p style="text-align: center;">$12 \div 3 = 4$</p>
----------------------------	--	--	---

Calculation Policy

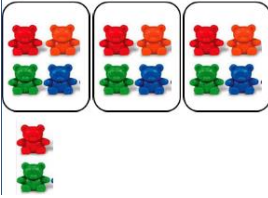
DIVISION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
S t a g e 1	<p>Division with no remainders through sharing. Use concrete materials to share into groups.</p> <p>$60 \div 3 = 20$ CONCRETE / PICTORIAL (Base 10 equipment)</p> <p>sharing</p>  <p>grouping</p> <p>$6 \text{ tens} \div 3 = 2 \text{ tens} = 20$</p> <p style="text-align: center;">$96 \div 3 = 32$</p> 	<p>Consolidate learning from KS1 using diagrams of sharing and repeated subtraction and addition on a number line to make jumps</p> <p>Example without remainder: $40 \div 5$ Ask "How many 5s in 40?"</p>  <p>Concrete methods could be represented pictorially within books to show understanding.</p>	<p>How many groups of 6 in 24?</p> <p style="text-align: center;">$24 \div 6 = 4$</p> <p>Abstract methods may be supported with pictorial methods within the children's books.</p>

Division with remainder through sharing

$14 \div 3 =$

Divide objects between groups and see how much is left over.



Division no remainders - introduction to bus stop method

Use place value equipment on a place value grid alongside short division.

Three examples of short division on place value grids: 4 into 8, 4 into 12, and 4 into 12 with a remainder of 2.

The model uses grouping.

Students can continue to use drawn diagrams with circles to help them divide numbers into equal groups. Remainders will be seen by not fitting into a whole group.

Draw dots and group them to divide an amount and clearly show a remainder.



Example without remainder:

40 ÷ 5. Ask "How many 5s in 40?" Diagram showing 8 groups of 5 on a number line from 0 to 40.

Example with remainder:

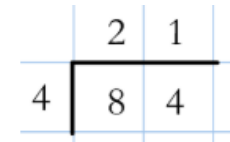
38 ÷ 6. Diagram showing 6 groups of 6 and a remainder of 2 on a number line from 0 to 38.

Children will begin to move onto division with remainders. A number sentence will support any abstract written calculation by using pictorial method to support.

29 ÷ 8 = 3 REMAINDER 5. Labels: dividend, divisor, quotient, remainder.

Short division

Children will begin to use the formal written method of division without remainders. This will only come after a clear concept is understood using manipulatives.



Dividing by 2,3,4, and 5

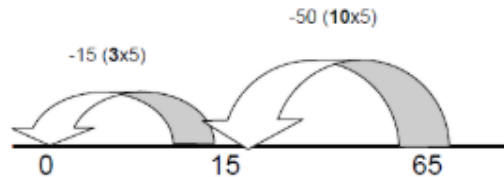
Division with remainders - Bus stop

$\begin{array}{r} 2 \\ 4 \overline{) 92} \end{array}$		<p>First, lay out the problem.</p>
$\begin{array}{r} 2 \\ 4 \overline{) 92} \end{array}$		<p>How many groups of 4 go into 9 tens? 2 groups of 4 tens with 1 ten left over.</p>
$\begin{array}{r} 2 \\ 4 \overline{) 92} \end{array}$		<p>Exchange the 1 ten left over for 10 ones. We now have 12 ones.</p>
$\begin{array}{r} 23 \\ 4 \overline{) 92} \end{array}$		<p>How many groups of 4 go into 12 ones? 3 groups of 4 ones.</p>

Pictorial representations can be used to support any concrete manipulatives.

	<p>How many groups of 6 are in 100?</p>	$6 \overline{) 100}$
	<p>How many groups of 6 are in 13 tens?</p>	$6 \overline{) 132}$
	<p>How many groups of 6 are in 12 ones?</p>	$6 \overline{) 132}$

Continue to use blank number lines as appropriate, using multiples of the divisor.
 $65 \div 5 = 13$



Chunking

Chunking is repeated subtraction of the divisor and multiples of the divisor.

$$73 \div 5$$

$\begin{array}{r} 5 \overline{) 73} \\ - 50 \\ \hline 23 \\ - 20 \\ \hline 3 \end{array}$	<p>(10 x 5)</p>	<p>10 + 4 = 14</p>
<p>(4 x 5)</p>		

How many 5s have been subtracted?
14 sets of 5, with 3 left over.

Answer: $73 \div 5 = 14 \text{ r}3$

Bus Stop Method for division

Begin with divisions that divide equally with no remainder.

$$\begin{array}{r} 218 \\ 4 \overline{) 872} \end{array}$$

Move onto divisions with a remainder.

$$\begin{array}{r} 86 \text{ r} 2 \\ 5 \overline{) 432} \end{array}$$

Calculation Policy

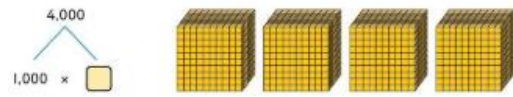
DIVISION - Upper KS2 (Years 5 & 6)

Concrete

Dividing whole numbers by 10, 100 and 1,000

Use place value equipment to support unitising for division.

$$4,000 \div 1,000$$



4,000 is 4 thousands.

$$4 \times 1,000 = 4,000$$

$$\text{So, } 4,000 \div 1,000 = 4$$

Concrete and pictorial representations may still be required to support the formal method of division (Bus Stop) - Go back to LKS2 to consolidate learning.

Pictorial

Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.

Th	H	T	O
3	2	0	0

$$3,200 \div 100 = ?$$

3,200 is 3 thousands and 2 hundreds.

$$200 \div 100 = 2$$

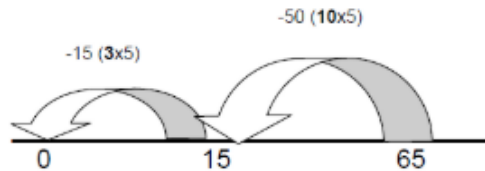
$$3,000 \div 100 = 30$$

$$3,200 \div 100 = 32$$

So, the digits will move two places to the right.

Continue to use blank number lines as appropriate, using multiples of the divisor.

$$65 \div 5 = 13$$

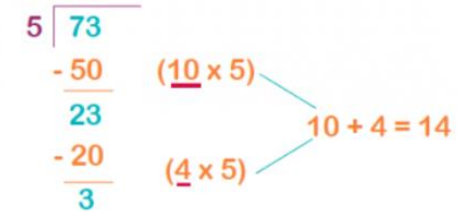


Abstract

Chunking

Chunking is repeated subtraction of the divisor and multiples of the divisor.

$$73 \div 5$$

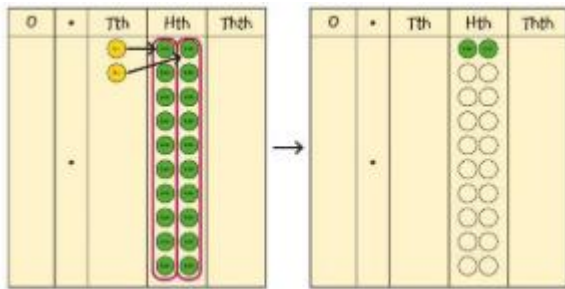


How many 5s have been subtracted?
14 sets of 5, with 3 left over.

$$\text{Answer: } 73 \div 5 = 14 \text{ r}3$$

Bus Stop Method for division

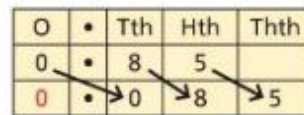
			<p>Begin with divisions that divide equally with no remainder.</p> $\begin{array}{r} 218 \\ 3 \overline{) 872} \end{array}$ <p>Move onto divisions with a remainder.</p> $\begin{array}{r} 86 \text{ r } 2 \\ 3 \overline{) 432} \end{array}$
S t a g e 2	<p>Dividing decimals by 10, 100 and 1,000 Use place value counters to represent dividing by 10, 100, 1000. Represent division using exchange on a place value grid.</p>	<p>Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.</p>	<p>Finally move into decimal places to divide the total accurately using a formal method for division (Bus stop)</p> $\begin{array}{r} 14.6 \\ 35 \overline{) 511.0} \end{array}$



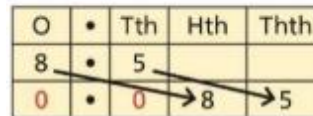
Exchange each 0.1 for ten 0.01s.

Divide 20 counters by 10.

0.2 is 2 tenths.
2 tenths is equivalent to 20 hundredths.
20 hundredths divided by 10 is 2 hundredths.



$$0.85 \div 10 = 0.085$$



$$8.5 \div 100 = 0.085$$

Long Division - Abstract Method

Calculations will start with tens and ones and move onto more advanced division calculations.

1. Divide.

$$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \end{array}$$

Two goes into 5 two times, or 5 tens $\div 2 = 2$ whole tens -- but there is a remainder!

2. Multiply & subtract.

$$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ \underline{-4} \\ 1 \end{array}$$

To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.

3. Drop down the next digit.

$$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ \underline{-4} \downarrow \\ 18 \end{array}$$

Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

